

# Effect Of Unsteady MHD Nanofluid In An Asymmetric Wavy Channel With Soret Effect

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## Abstract

Flow through asymmetric wavy channel is important in electronics coolant in industry and biomedical industry. Numerous investigations have been reported presenting analytical and numerical solutions for a plethora of different geometrical scenarios, such flows are important in rocket propulsion control, crystal growth technology, astrophysical plasma fluid dynamics, tri-biological regulation in moving machine parts and magnetohydrodynamic energy generators. An electrically conducting oscillatory incompressible nanofluid past a asymmetric wavy channel bounded by a porous medium is considered. Appropriate boundary conditions are considered on the boundary of the wavy channel. The nano fluid effects in velocity profile, temperature profile and concentration profile for various parameters are plotted with graphs. Heat and mass transfer effects are analyzed.

## 1 Introduction

The effects in a wavy wall channel using forced convection was studied by Wang and Chen [12]. Oscillatory flow in an asymmetric wavy channel with magnetic effect was discussed by Sudharsan Reddy *et al.* [11]. The same work in irregular channel with chemical reaction was analyzed by Satya Narayana *et al.* [10]. Soret effect for a wavy channel was discussed by Sasikumar *et al.*[9]. Magnetohydrodynamic flow in rotating systems continues to stimulate significant research in the fields of engineering science and applied mathematics.

Dragon and Grotberg [3] studied the mass transport in a flexible tube with oscillatory flow in the year 1991. Oscillatory Stokes flow in porous media was discussed by Chapman and Higdon [1]. Many studies were gone through the field of oscillatory flow through porous media in the year 2000. Later, Graham and Higdon [4] worked on the oscillatory forcing of flow through porous media. Looker and Carnie [7] discussed the hydrodynamics of an oscillating porous sphere. An exact solution of oscillatory flow through a porous medium in sphere was discussed by Loganathan and Prathiba[5],[6]. Magnetohydrodynamic flow past a rotating cylinder was derived by Prathiba *et al.* [8]. Axial dispersion in packed beds of spheres was done by Crittenden *et al.* [2].

Oscillatory flow through many objects has gained importance lately since it is used in industry and geophysical applications. With a vast array of potential applications, it is fairly evident that a lot of people have put in their minds and thoughts, trying to invent more innovations in this prevalent field. Nano particles have introduced to increase the transfer of heat in the fluid. Many methods are used to progress current of the fluids by dangling nano particles in waters.

Recently the flow of fluids in an asymmetric porous wavy channel was studied by many researchers. In this paper the heat and mass transfer, soret effect on magnetohydrodynamic

oscillatory flow of nanofluid through porous medium in asymmetric wavy channel is analysed. The nanofluid effects in velocity contour, temperature profile and concentration profile for various parameters are discoursed. Heat and mass transfer of several parameters are analysed.

## 2 Governing equations of the problem

Consider the electrically conducting nano fluid with the viscous incompressible flow in a asymmetric wavy channel bounded by the permeable medium.

The wall surface is defined as

$$H_L = d_1 + a_1 \cos \left[ \frac{2\pi}{\lambda} (x) \right] \quad (1)$$

$$H_R = -d_2 - a_2 \cos \left[ \frac{2\pi}{\lambda} (x) + \phi \right] \quad (2)$$

where  $a_1$  and  $a_2$  are the amplitude of the left and right of the walls and ,  $d_1$  and  $d_2$  are the half width of the channel,  $\lambda$  is the wave length ,  $\phi$  is the phase difference,  $\phi$  varies from 0 to  $\pi$  and also have the relation

$$a_1^2 + a_2^2 + 2a_1a_2 \cos(\phi) \leq (d_1 + d_2) \quad (3)$$

$T_1$  and  $T_2$  are the temperature of the two walls. Magnetic field is applied normal to the walls.

The governing equation of the nanofluid flow are given by

$$\rho_{nf} \left( \frac{\partial u}{\partial t} \right) = -\frac{\partial p}{\partial x} + \mu_{nf} \frac{\partial^2 u}{\partial y^2} - \sigma B_0^2 u - \frac{\mu_{nf}}{K} u + (\rho\beta_T)_{nf} g(T - T_2) + (\rho\beta_C)_{nf} g(C - C_2) \quad (4)$$

$$(\rho C_p)_{nf} \frac{\partial T}{\partial t} = K_{nf} \frac{\partial^2 T}{\partial y^2} - \frac{\partial q}{\partial y} + Q^*(T - T_2) \quad (5)$$

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial y^2} - K_r^*(C - C_2) + \frac{DK_T}{T_m} \frac{\partial^2 T}{\partial y^2} \quad (6)$$

where  $u$  - velocity component along x axis.  $\rho_{nf}$  - nanofluid density ,  $\mu_{nf}$  - nanofluid viscosity ,  $\sigma$  - electric conductivity of the fluid,  $B_0$  - uniform magnetic field,  $g$  - acceleration due to gravity,  $(\beta_T)_{nf}$  - coefficient of thermal expansion of nanofluid,  $(\beta_C)_{nf}$  - coefficient of mass expansion of nanofluid,  $T$  - temperature of the nanofluid,  $T_0$  - temperature ,  $C$  - concentration of the nanofluid,  $C_0$  - concentration,  $(\rho C_p)_{nf}$  - heat capacity of the nanofluid,  $k$  - permeable parameter,  $q$  - radiative heat flux,  $K_r^*$  - chemical reaction parameter,  $Q^*$  - heat source parameter and  $D$  - mass diffusion coefficient.

Hamilton and Crosser defined the effective properties of the nanofluid as

$$\rho_{nf} = (1 - \phi)\rho_f + \phi\rho_s \quad (7)$$

$$(\rho\beta)_{nf} = (1 - \phi)(\rho\beta)_f + \phi(\rho\beta)_s \quad (8)$$

$$(\rho C_p)_{nf} = (1 - \phi)(\rho C_p)_f + \phi(\rho C_p)_s \quad (9)$$

$$\mu_{nf} = \frac{\mu_f}{(1 - \phi)^{2.5}} \quad (10)$$

$$K_{nf} = K_f \left( \frac{K_s + 2K_f - 2\phi(K_f - K_s)}{K_s + 2K_f + 2\phi(K_f - K_s)} \right) \quad (11)$$

$$\alpha_{nf} = \frac{K_{nf}}{(\rho C_p)_{nf}} \quad (12)$$

where  $\rho_s$  and  $\rho_f$  are the solid and fluid particles densities of the respectively.  $\beta_s$  and  $\beta_f$  are the solid and fluid coefficients of thermal expansion respectively.  $\alpha_{nf}$  - thermal diffusivity.  $K_f$  and  $K_s$  - base fluid and solid conductivities respectively.  $\phi$  is the solid volume fraction of nanofluid.

The heat flux and the pressure gradient be

$$\frac{\partial q}{\partial y} = 4\alpha^2(T_2 - T) \quad (13)$$

$$-\frac{\partial P}{\partial x} = \lambda e^{int'} \quad (14)$$

where  $\alpha$  - mean radio activity absorption coefficient and  $n$  - frequency of oscillation.

Boundary conditions are

$$y = H_L: u = 0, T = T_1, C = C_1 \quad (15)$$

$$y = H_R: u = 0, T = T_2, C = C_2 \quad (16)$$

The non dimensional quantities are

$$u' = \frac{u}{U}, x' = \frac{x}{\lambda}, y' = \frac{y}{d}, a = \frac{a_1}{d_1}, b = \frac{b_1}{d_1}, d = \frac{d_2}{d_1}, H_L = \frac{h_1}{d_1}, H_R = \frac{h_2}{d_1}, t' = \frac{Ut}{d}$$

$$s^2 = \frac{1}{D_a}, D_a = \frac{K_f}{d^2}, Q = \frac{Q^* d^2}{K_f}, K_r = \frac{dK_r^*}{U}, S_r = \frac{DK_T (T_1 - T_2)}{T_m d U (C_1 - C_2)}, M^2 = \frac{\sigma B_0^2 d^2}{\mu_f},$$

$$G_r = \frac{g(\beta_T)_f d^2 (T_1 - T_2)}{\nu_f U}, G_c = \frac{g(\beta_c)_f d^2 (C_1 - C_2)}{\nu_f U}, p' = \frac{pd^2}{\mu_f \lambda U}, P_e = \frac{U d (\rho C_p)_{nf}}{K}$$

$$S_c = \frac{D}{U d}, R_e = \frac{U d}{\nu_f}, N^2 = \frac{4\alpha^2 d^2}{K}, \theta = \frac{(T - T_2)}{(T_1 - T_2)}, \phi = \frac{(C - C_2)}{(C_1 - C_2)} \quad (17)$$

where  $U$  is the mean flow velocity,  $G_r$  is Grashof number,  $G_m$  is modified Grashof number,  $R_e$  is the Reynolds number,  $P_e$  is the Peclet number,  $D_a$  is the Darcy number,  $S_r$  is Soret number,  $Q$  is heat source,  $K_r$  - chemical reaction parameter,  $N$  is radiation parameter and  $S_c$  is Schmidt number.

Using the non dimensional terms

$$R_e \frac{\partial u'}{\partial t'} = \lambda e^{int'} + \frac{\partial^2 u'}{\partial y'^2} + G_r \theta + G_c \phi - (s^2 + M^2) u' \quad (18)$$

$$P_e \frac{\partial \theta}{\partial t'} = \frac{\partial^2 \theta}{\partial y'^2} + (N^2 + Q) \theta \quad (19)$$

$$\frac{\partial \phi}{\partial t'} = S_c \frac{\partial^2 \phi}{\partial y'^2} - K_r \phi - S_r \frac{\partial^2 \theta}{\partial y'^2} \quad (20)$$

The corresponding non dimensional boundary conditions are

$$u' = 0, \theta = 1, \phi = 1 \quad \text{at } y' = h_1 \quad (21)$$

$$u' = 0, \theta = 0, \phi = 0 \quad \text{at } y' = h_2 \quad (22)$$

### 3 Solution of the Problem

For solving the equations, assume that

$$u(y', t') = u_0(y')e^{int'} \quad (23)$$

$$\theta(y', t') = \theta_0(y')e^{int'} \quad (24)$$

$$\phi(y', t') = \phi_0(y')e^{int'} \quad (25)$$

Now substituting equations (23) - (25) in equations (18)-(20)

$$\frac{d^2 u_0}{dy'^2} - (R_e in + M^2 + s^2)u_0 = -(G_r \theta_0 + G_c \phi_0 - \lambda) \quad (26)$$

$$\frac{d^2 \theta_0}{dy'^2} + (N^2 + Q - P_e in)\theta_0 = 0 \quad (27)$$

$$S_c \frac{d^2 \phi_0}{dy'^2} + S_r \frac{d^2 \theta_0}{dy'^2} - (K_r + in)\phi_0 = 0 \quad (28)$$

Substituting equation (27) in equation (28), then equation (28) becomes

$$\frac{d^2 \phi_0}{dy'^2} + \frac{S_r}{S_c} (N^2 + Q - P_e in)\theta_0 - \frac{(K_r + in)}{S_c} \phi_0 = 0 \quad (29)$$

And the boundary conditions are

$$u_0 = 0, \theta_0 = 1, \phi_0 = 1 \quad \text{at } y = h_1 \quad (30)$$

$$u_0 = 0, \theta_0 = 0, \phi_0 = 0 \quad \text{at } y = h_2 \quad (31)$$

Solving equations (26),(27) and (29) along with the boundary conditions (30) and (31), then

$$u_0 = A_3 e^{E_3 y'} + A_4 e^{-E_3 y'} - \frac{1}{E_3^2} (\lambda - G_r \theta_0 - G_c \phi_0) \quad (32)$$

$$\theta_0 = \frac{\sin E_1 (h_2 - y')}{\sin E_1 (h_2 - h_1)} \quad (33)$$

$$\phi_0 = A_1 e^{E_2 y'} + A_2 e^{-E_2 y'} + \left(\frac{S_r}{S_c}\right) \left(\frac{E_1^2}{E_2^2}\right) \theta_0 \quad (34)$$

Using equations (23) -(25), then equations (32)-(34) becomes

$$u = \left[ A_3 e^{E_3 y'} + A_4 e^{-E_3 y'} - \left(\frac{\lambda}{E_3^2}\right) + \left(\frac{G_r}{E_3^2}\right) \left(\frac{\sin E_1 (h_2 - y')}{\sin E_1 (h_2 - h_1)}\right) - \left(\frac{G_c}{E_3^2}\right) \left( A_1 e^{E_2 y'} + A_2 e^{-E_2 y'} + \left(\frac{S_r}{S_c}\right) \left(\frac{E_1^2}{E_2^2}\right) \left(\frac{\sin E_1 (h_2 - y')}{\sin E_1 (h_2 - h_1)}\right) \right) \right] e^{int'} \quad (35)$$

$$\theta = \left[ \frac{\sin E_1 (h_2 - y')}{\sin E_1 (h_2 - h_1)} \right] e^{int'} \quad (36)$$

$$\phi = \left[ A_1 e^{E_2 y'} + A_2 e^{-E_2 y'} + \left( \frac{S_r}{S_c} \right) \left( \frac{E_1^2}{E_2^2} \right) \left( \frac{\sin E_1 (h_2 - y')}{\sin E_1 (h_2 - h_1)} \right) \right] e^{int'} \quad (37)$$

#### 4 Shear Stress

The shear stress is

$$\tau = -\mu \left( \frac{\partial u}{\partial y'} \right)_{y=h_1, h_2}$$

$$\tau = -\mu \left[ \left[ A_3 e^{E_3 y'} E_3 - A_4 e^{-E_3 y'} E_3 - E_1 \left( \frac{G_r}{E_3^2} \right) \left( \frac{\cos E_1 (h_2 - y')}{\sin E_1 (h_2 - h_1)} \right) - \left( \frac{G_c}{E_3^2} \right) \left( A_1 e^{E_2 y'} E_2 - A_2 e^{-E_2 y'} E_2 - E_1 \left( \frac{S_r}{S_c} \right) \left( \frac{E_1^2}{E_2^2} \right) \left( \frac{\cos E_1 (h_2 - y')}{\sin E_1 (h_2 - h_1)} \right) \right) \right] e^{int'} \right]_{y=h_1, h_2} \quad (38)$$

#### 5 Heat Transfer

The rate of heat transfer

$$Nu = - \left[ \frac{\partial \theta}{\partial y'} \right]_{y'=h_1, h_2}$$

$$Nu = E_1 \left[ \left[ \frac{\cos E_1 (h_2 - y')}{\sin E_1 (h_1 - h_2)} \right] e^{int'} \right]_{y'=h_1, h_2} \quad (39)$$

#### 6 Mass Transfer

The rate of mass transfer

$$Sh = - \left[ \frac{\partial \phi}{\partial y'} \right]_{y'=h_1, h_2}$$

$$Sh = \left[ \left[ A_2 e^{-E_2 y'} E_2 - A_1 e^{E_2 y'} E_2 + E_1 \left( \frac{S_r}{S_c} \right) \left( \frac{E_1^2}{E_2^2} \right) \left( \frac{\cos E_1 (h_2 - y')}{\sin E_1 (h_2 - h_1)} \right) \right] e^{int'} \right]_{y'=h_1, h_2} \quad (40)$$

#### 7 Results and Discussion

The various parameter of the nanofluid past asymmetric wavy channel is discussed. The velocity profile for various parameters are studied using different values. The results are obtained for the flows by using the Fig.1 to Fig.21.

Velocity profiles are exposed in Fig.3.1 to Fig.3.8. In Fig.1 velocity declines for growing values of the parameter Gc and with the remaining parameters are M=1, N=2, Q=2, Sc=0.6, Re=1, λ=1, Pe=0.1, Gr=2, Sr=1 and s=1. From Fig.2, it is realized that the velocity gradually declines with growing Schmidt number with the remaining parameters M=1, N=2, Q=2, Gc=1, Re=1, λ=1, Pe=0.1, Gr=2, Sr=1 and s=1. For increasing N the velocity becomes increases steadily. These results are existing in fig.3 and the lasting parameters are parameters M=1, Q=2, Gc=1, Re=1, λ=1, Pe=0.1, Gr=2, Sr=1 and s=1. For increasing magnetic parameter M the velocity becomes declines. These results are present in fig.4 and the remaining parameters are same in the previous figure.

For increasing  $Pe$  the velocity becomes increases for some radius , after certain period it is gradually decreasing. These results are present in fig.5 and the remaining parameters are same in the previous figure. The behaviour of Grashof number in velocity profile is noticeable. Velocity increases for Grashof number and the variation are large. That is shown in Fig.6. When a graph is plotted between velocity and radial distance of the wavy channel , (Fig.7) velocity rises with increase Soret number. Fig.8 represents velocity profile for several values of the permeability. Here velocity profile intensifications with increasing  $Q$  and the remaining parameters are  $Pe=0.1$ ,  $Gc=1$ ,  $Sc=0.6$ ,  $Re=1$ ,  $Gr=2$ ,  $N=2$ ,  $Sr=1$ .

Temperature profiles are represented in Fig.9 to Fig.14. From Fig.9, we see that there is no noteworthy change for different values of  $Gc$ . Temperature decreases for increasing Peclet number and the rate of decrement is in Fig.10. Then for higher  $y$ , a slight slope is in the Peclet number, just like the one seen in Fig.8. For negative values of  $Q$  temperature declines for reducing values of heat source and the remaining parameters are  $Pe=0.1$ ,  $Gc=1$ ,  $Sc=0.3$ ,  $Re=1$ ,  $Gr=2$ ,  $N=2$ ,  $Sr=1$  that is in Fig.11.If a graph is designed against temperature to  $N$  (Fig.12) in the occurrence of a permeability and magnetic parameter, the increase rate of  $N$  leads to the temperature to decrease. In Fig.13. temperature diminutions for growing numbers of positive  $Q$ , with  $Pe=0.1$ ,  $Gc=1$ ,  $Sc=0.3$ ,  $Re=1$ ,  $Gr=2$ ,  $N=2$ ,  $Sr=1$ . Temperature decreases as the values of  $x$  magnetic parameter rises and  $x$  reaches a single value for some  $y$  is presented in Fig.14.

Concentration profile is studied from Fig.15 to Fig.19. In Fig.15 concentration is decreases and tends to a single value for different increasing value of the frequency parameter. If  $Sc$  is increases, the concentration profile mostly upsurges with rising  $y$ , then for higher  $Sc$ , a small slump is initiate in concentration profile, as seen in Fig.16. The behaviour of concentration profile is slightly different for various values of  $Q$ . It gradually decreases for increasing values of  $Q$  is shown in Fig.17. Again, for the varying Peclet values, concentration decreases and suddenly raises for higher  $y$ , reaches a single value for some  $y$ , as represented in Fig.18. And, for the varying Soret values, concentration increases, for higher values the raise in concentration profile is very high and suddenly reduced to some common value, as represented in Fig.19.

Shear stress is represented in Fig.20 and Fig.21. As seen in Fig.20, shear stress declines as the Schmidt number rises with  $Pe=0.3$ ,  $Gc=1$ ,  $Q=2$ ,  $Re=1$ ,  $Gr=2$ ,  $N=2$ ,  $Sr=1$ . Once a chart is designed for different values of Peclet number (Fig.21), initially skin friction increases for increasing Peclet number but for higher values of  $y$  it decreases.

The rate of heat transfer is denoted in Fig.22 and Fig.23. As understood in Fig.22, heat transfer raises as the radiation parameter upsurges with  $Pe=0.3$ ,  $Gc=1$ ,  $Q=2$ ,  $Re=1$ ,  $Gr=2$ ,  $Sc=0.6$ ,  $Sr=1$ . For various values of  $Q$  (Fig.23), heat transfer decreases and differences are very clear with very small  $N$  and the remaining values are  $Pe=0.3$ ,  $Gc=1$ ,  $N=0.1$ ,  $Re=1$ ,  $Gr=2$ ,  $Sc=0.6$ ,  $Sr=1$ . Fig.24 is for mass transfer with different Schmidt number. When ever the Schmidt number upsurges the mass transfer rises gradually.

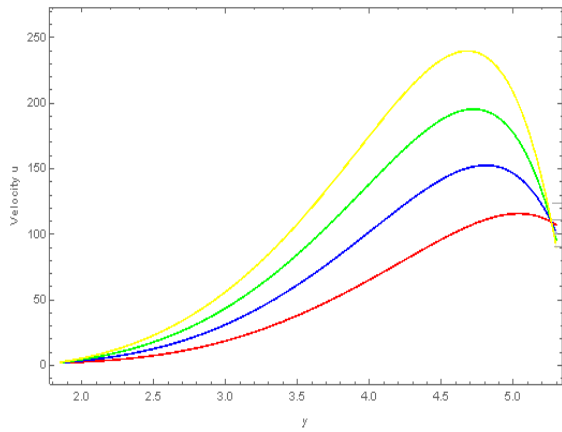


Fig.1 Velocity profile for various values of  $G_c$  with  $M=1, Sc=0.6, Re=1, Pe=0.1, Gr=2, Sr=1, N=2$

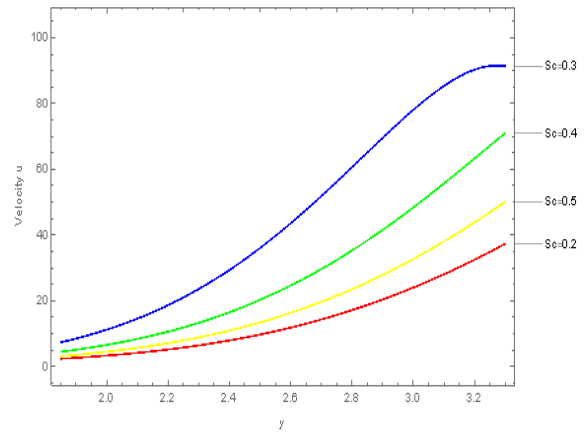


Fig.2 Velocity profile for various values of  $Sc$  with  $M=1, G_c=1, Re=1, Pe=0.1, Gr=2, Sr=1, N=2$

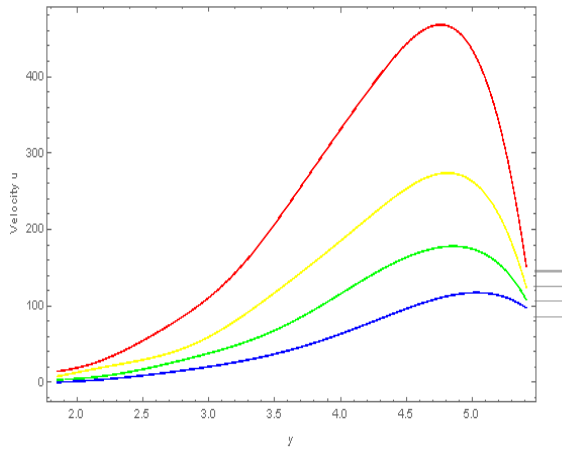


Fig.3 Velocity profile for various values of  $N$  with  $M=1, G_c=1, Re=1, Pe=0.1, Gr=2, Sr=1, Sc=0.6$

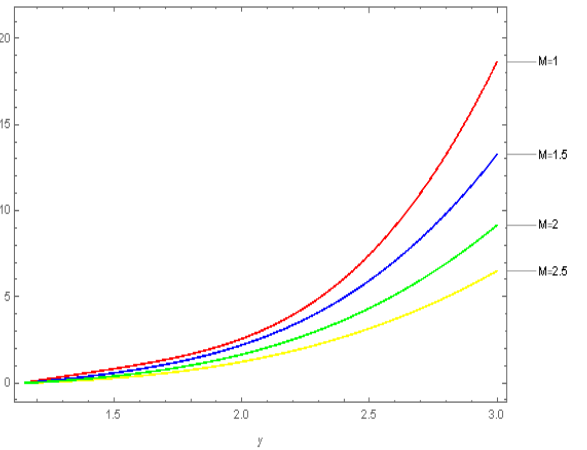


Fig.4 Velocity profile for various values of  $M$  with  $Sc=0.6, G_c=1, Re=1, Pe=0.1, Gr=2, Sr=1, N=2$

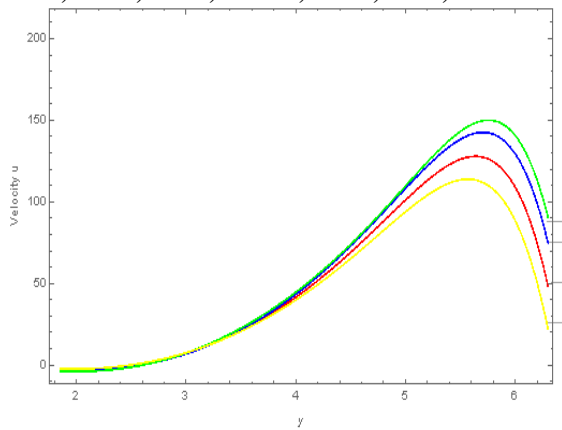


Fig.5 Velocity profile for various values of  $Pe$  with  $M=1, G_c=1, Re=1, Sc=0.6, Gr=2, Sr=1, N=2$

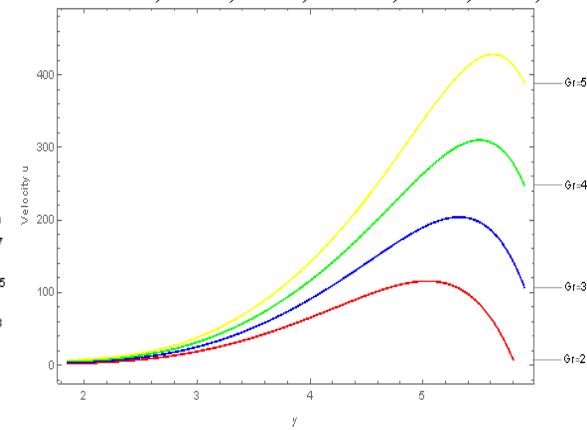
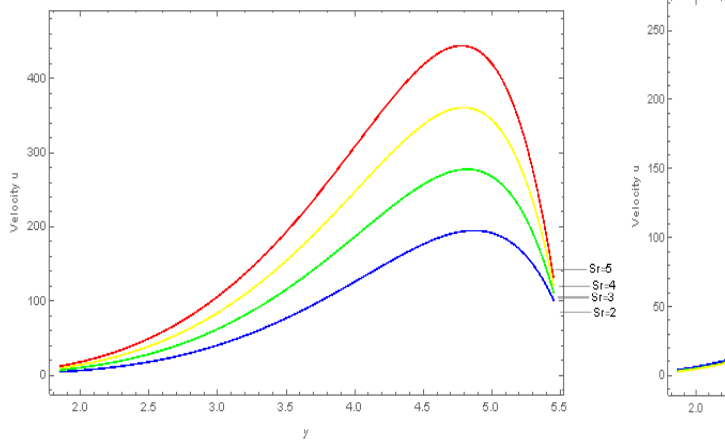
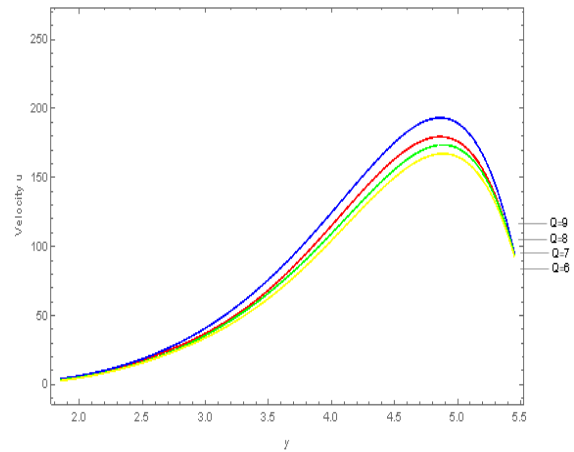


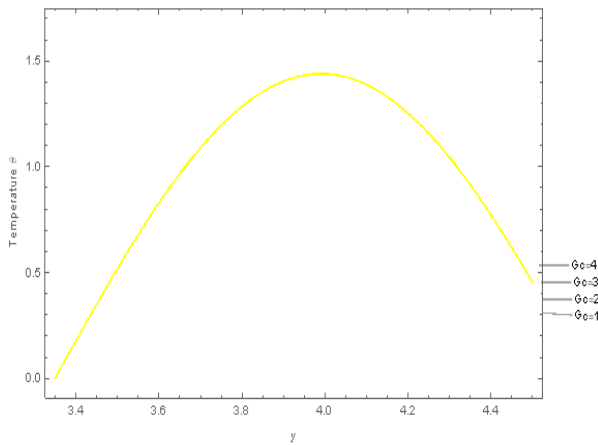
Fig.6 Velocity profile for various values of  $Gr$  with  $M=1, G_c=1, Re=1, Pe=0.1, Sc=0.6, Sr=1, N=2$



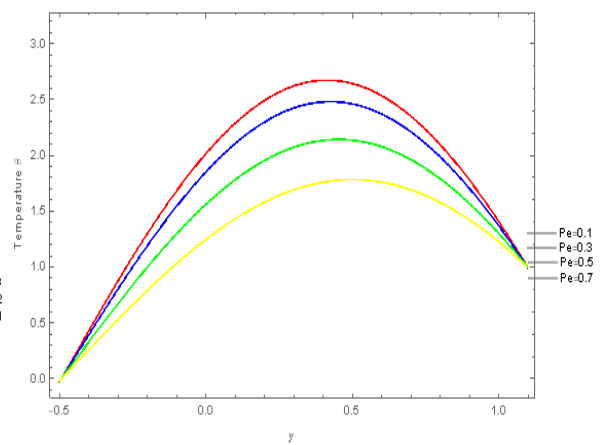
**Fig.7 Velocity profile for various values of Sr with M=1, Gc=1, Re=1, Pe=0.1, Gr=2, Sc=0.6, N=2**



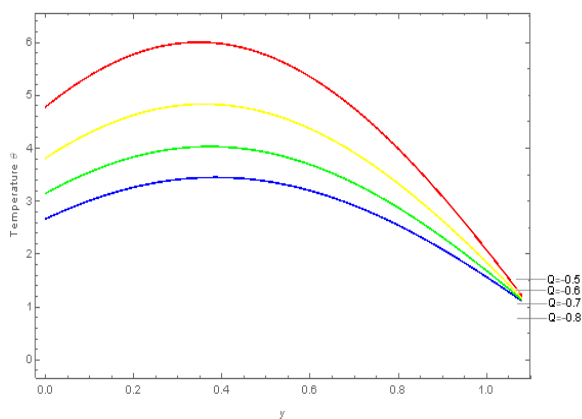
**Fig. 8 Velocity profile for various values of Q with M=1, Gc=1, Re=1, Pe=0.1, Gr=2, Sr=1, N=2, Sc=0.6**



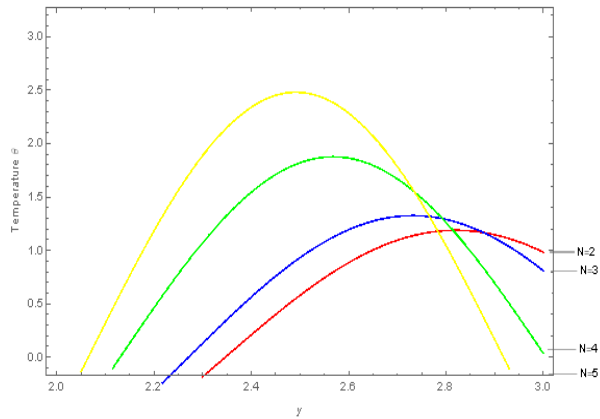
**Fig.9 Temperature profile for various values of Gc with M=1, Q=2, Re=1, Pe=0.1, Gr=2, Sr=1, Sc=0.6**



**Fig.10 Temperature profile for various values of Pe with M=1, Q=2, Re=1, Gc=1, Gr=2, Sr=1, Sc=0.6**

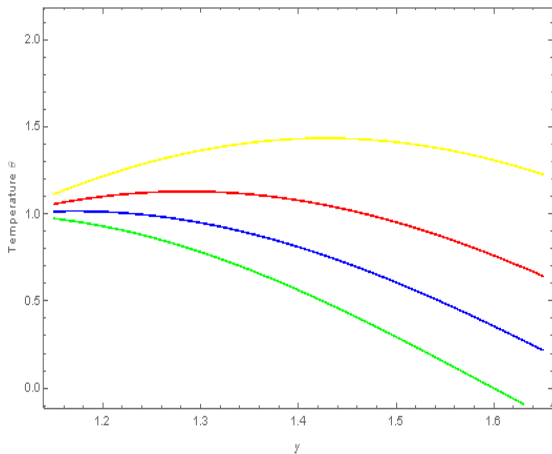


**Fig.11 Temperature profile for various values of negative Q with M=1, Pe=0.1, Re=1, Gc=1, Gr=2, Sr=1, N=2, Sc=0.6**

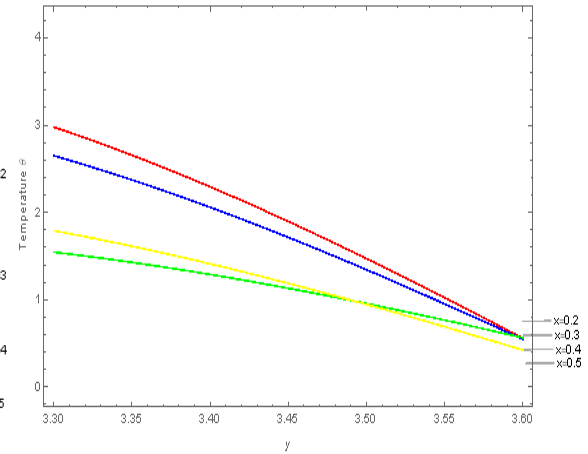


**Fig.12 Temperature profile for various values of N with M=1, Pe=0.1, Re=1, Gc=1, Gr=2, Sr=1, Q=2, Sc=0.6**

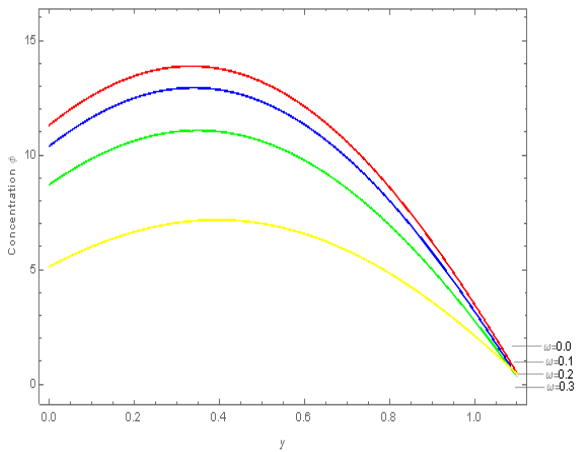




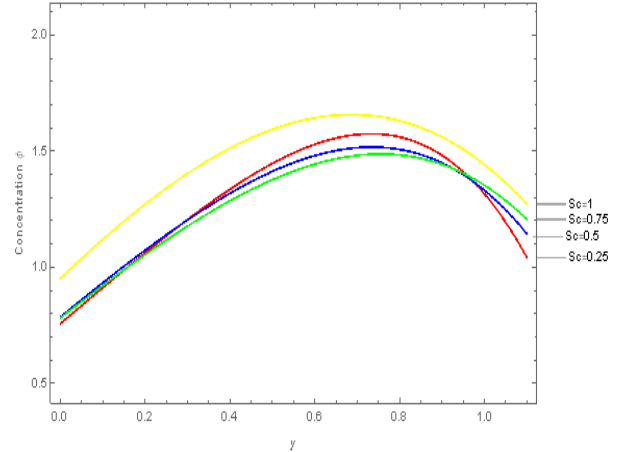
**Fig.13** Temperature profile for various values of  $Q$  with  $M=1, Pe=0.1, Re=1, Gc=1, Gr=2, Sr=1, N=2, Sc=0.6$



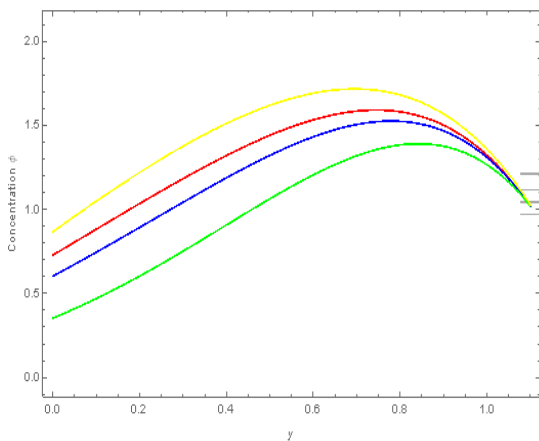
**Fig.14** Temperature profile for various values of  $x$  with  $M=1, Pe=0.1, Re=1, Gc=1, Gr=2, Sr=1, N=2, Sc=0.6, Q=2$



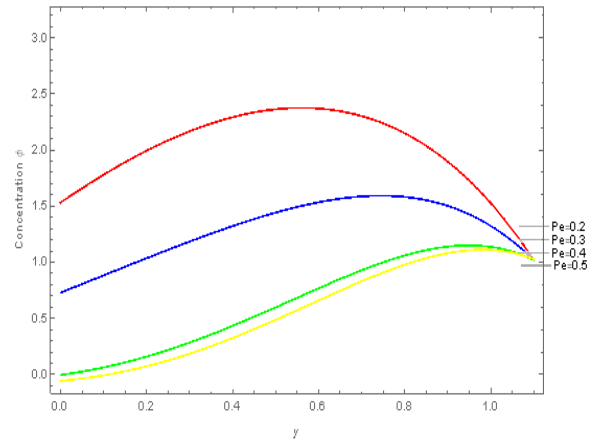
**Fig.15** Concentration profile for various values of  $w$  with  $M=1, Pe=0.3, Re=1, Gc=1, Gr=2, Sr=1, N=2, Sc=1, Q=2$



**Fig.16** Concentration profile for various values of  $Sc$  with  $M=1, Pe=0.3, Re=1, Gc=1, Gr=2, Sr=1, N=2, Q=2$

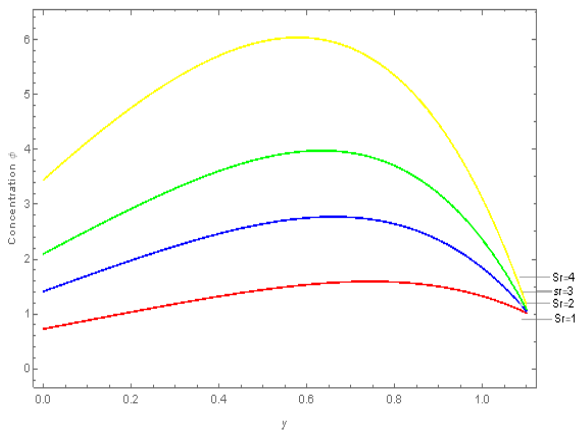


**Fig.17** Concentration profile for various values of  $Q$  with  $M=1, Pe=0.3, Re=1, Gc=1, Gr=2, Sr=1, N=2,$



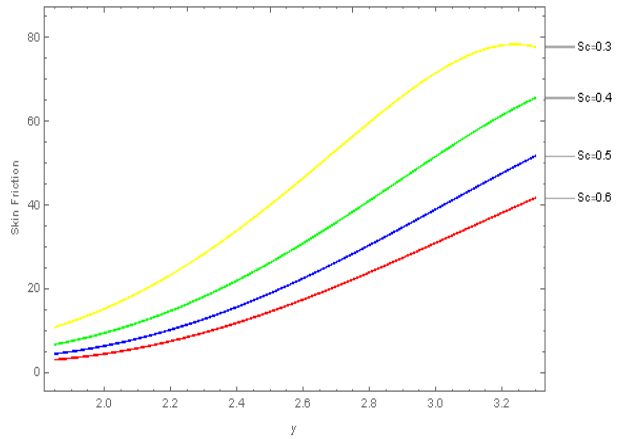
**Fig.18** Concentration profile for various values of  $Pe$  with  $M=1, Re=1, Gc=1, Gr=2, Sr=1, N=2,$

**Q=2, Sc=0.2**

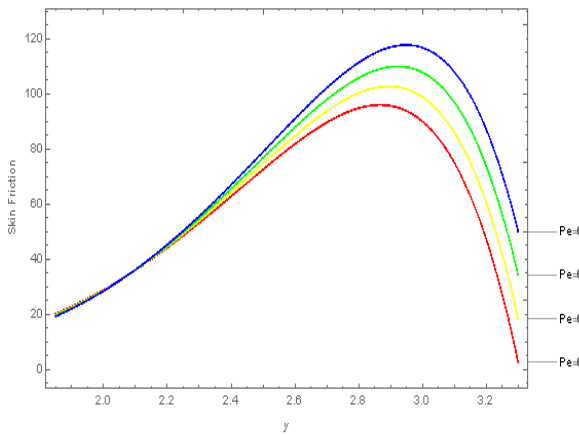


**Fig.19 Concentration profile for various values of  $Sr$  with  $M=1, Pe=0.3, Re=1, Gc=1, Gr=2, Sr=1, N=2, Q=2, Sc=0.2$**

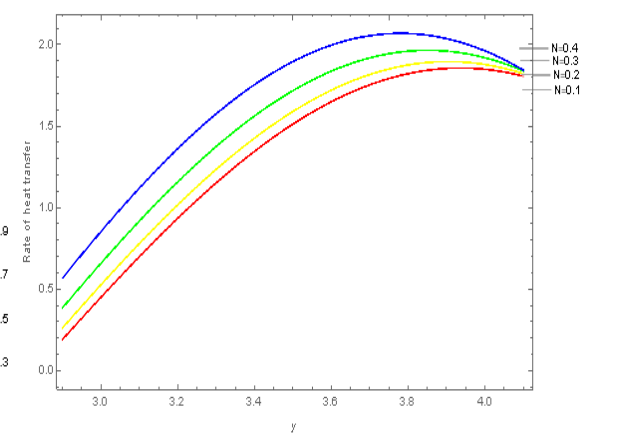
**Q=2, Sc=0.2**



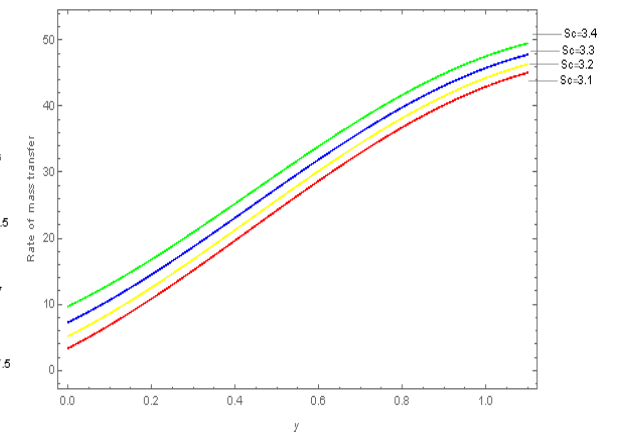
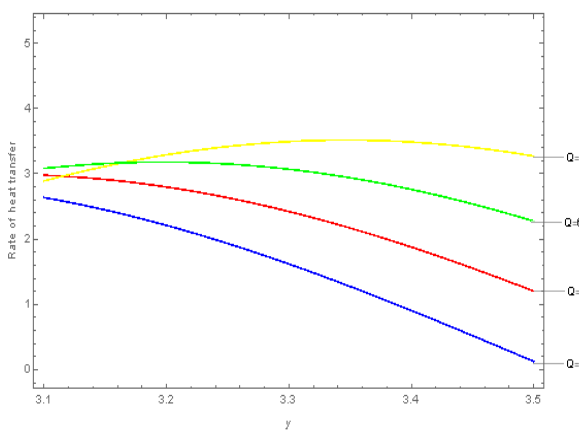
**Fig.20 Skin friction for various values of  $Sc$  with  $M=1, Re=1, Gc=1, Gr=2, Pe=0.3, N=2, Q=2, Sr=1$**



**Fig.21 Skin friction for various values of  $Pe$  with  $M=1, Re=1, Gc=1, Gr=2, Sc=0.2, N=2, Q=2, Sr=1$**



**Fig.22 Heat transfer for various values of  $N$  with  $M=1, Re=1, Gc=1, Gr=2, Sc=0.6, Pe=0.1, Q=2, Sr=1$**



**Fig.23 Heat transfer for various values of Q with M=1, Re=1, Gc=1, Gr=2, Sc=0.6, Pe=0.1, N=0.1, Sr=1**

**Fig.24 Mass transfer for various values of Sc with M=1, Re=1, Gc=1, Gr=2, Q=2, Pe=0.2, N=1, Sr=1**

## Appendix

$$E_1 = \sqrt{N^2 + Q - Pe \, in}$$

$$E_2 = \sqrt{\frac{K_r + in}{S_c}}$$

$$E_3 = \sqrt{S^2 + M^2 - Re \, in}$$

$$A_1 = \left( \frac{1}{S_c E_2^2} \right) \left( \frac{S_c E_2^2 - S_r E_1^2}{e^{E_2 h_1} - e^{2E_2 h_2}} \right)$$

$$A_2 = -A_1 e^{2E_2 h_2}$$

$$A_3 = \frac{\frac{\lambda}{E_3^2} (e^{E_3 (h_2 - h_1)} - 1) + \frac{Gr}{E_3^2} + \frac{G_c}{E_3^2}}{e^{E_3 h_1} - e^{E_3 (2h_2 - h_1)}}$$

$$A_4 = \frac{\lambda}{E_3^2} e^{E_3 h_2} - A_3 e^{2E_3 h_2}$$

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